# Novel Monte Carlo study of deposited magnetic nanoparticles



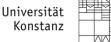
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 $[\mu_{\rm B}]$ 

1.74

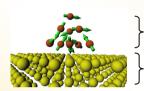
1.82

1.87

1.88

#### Introduction

- In order to study the finite temperature behavior of magnetic nanoparticles, a novel Monte Carlo method has been developed. The energy of a new trial configuration during the simulation is calculated directly from the expansion of the band energy avoiding the set up of an a priori Heisenberg-type model.
- Studies of deposited magnetic nanoparticles



magnetic cluster.

non-magnetic (semi-infinite) host. e.g., Au(111), Cu(001)

The magnetic properties of a wide class of systems are often described by the classical Heisenberg model.

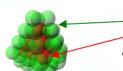
$$\mathcal{H} = rac{1}{2} \sum_{i,j} J_{ij} \boldsymbol{\sigma}_i \boldsymbol{\sigma}_j - \sum_i K\left(\boldsymbol{\sigma}_i^z\right)^2,$$

where isotropic coupling between spins and uniaxial anisotropy are considered. We compare the ab initio and the Heisenberg model based temperature dependence of the magnetic moment of a Co<sub>4x4</sub>|Cu(001) cluster, and find good agreement for this particular case.

### Computational method I. - Electronic structure

- Electronic structure calculation: fully relativistic implementation of the local spindensity approximation of the density functional theory
- Embedded cluster Green's function technique based on the KKR method [1]

$$\boldsymbol{\tau}(\varepsilon) = \boldsymbol{\tau}_{\text{host}}(\varepsilon) \left( \mathbf{I} - \Delta \mathbf{t}^{-1}(\varepsilon) \boldsymbol{\tau}_{\text{host}}(\varepsilon) \right)^{-1}$$



environment (vacuum or host atoms) real cluster (e.g., Cr or Co atoms)

- Self-consistent cluster calculation
- then: frozen potential approximation
- Taylor-expansion of the band energy:

$$E_b \approx E_0 + \sum_{i=1}^{N} \frac{\partial E_b}{\partial \sigma_i} \bigg|_{\{\boldsymbol{\sigma}_0\}} \Delta \boldsymbol{\sigma}_i + \frac{1}{2} \sum_{i,j=1}^{N} \Delta \boldsymbol{\sigma}_i^{\mathrm{T}} \frac{\partial^2 E_b}{\partial \sigma_i \partial \boldsymbol{\sigma}_j} \bigg|_{\{\boldsymbol{\sigma}_0\}} \Delta \boldsymbol{\sigma}_j$$

• The derivatives of the band energy can be calculated analytically from Lloyd's formula, see [2].

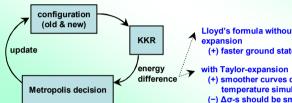
$$E_b = -\frac{1}{\pi} \operatorname{Im} \int_{-\infty}^{\varepsilon_F} \operatorname{Tr} \ln \boldsymbol{\tau}(\varepsilon) \, \mathrm{d}\varepsilon$$

## Computational method II. - Monte Carlo simulation

- Ground state by simulated annealing
- Finite temperature simulation
- We used the Metropolis algorithm with single spin flip dynamics:

$$P(i \to f) = \begin{cases} 1, & \text{if } E_f \le E_i, \\ e^{-\beta(E_f - E_i)}, & \text{if } E_f > E_i. \end{cases}$$

Flowchart of the code:



Llovd's formula without Taylor-

- (+) faster ground state search
- (+) smoother curves during finite temperature simulation
- (-) Δσ-s should be small enough

## Results I. - Ground state of AFM and FM clusters

 Benchmark system: Cr trimer on Au(111) surface. The same ground state was found in [3] by solving the Landau-Lifshitz-Gilbert equations.



cluster on Au(111) surface

frustration non-collinear

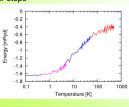
Ground state of a pyramid shaped Cr.

(side view)





 Simulated annealing of this cluster in four steps

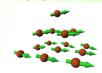


■ Tetrahedron shaped Cr particle on Au(111) surface, Similar ground state was found in [4] for the same Cr cluster on Cu(111) surface.

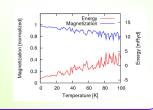


collinear ground state

 Ground state of a pyramid shaped Co... cluster on Cu(001) surface

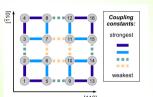


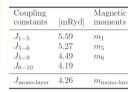
Simulated annealing of this cluster



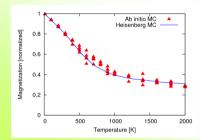
# Results II. - Thermodynamics of a Co<sub>4×4</sub>|Cu(001) cluster

Geometry and isotropic coupling constants between next nearest neighbors





Square root of the thermal average of the square of the magnetization:



> In the Heisenberg MC simulation, we used 105 MC steps per temperature points and the anisotropy constant of the monolayer cobalt on Cu(001) surface. K = 0.0228 mRvd: > in the ab initio MC simulation we used 5 x 104 MC

steps per temperature points.

### **Future plans**

- Simulating an "STM tip" and investigating the distancedependence of its magnetic structure and ground state
- Further studies of the thermodynamics of magnetic nanoparticles (magnetic switching)



## References and acknowledgments

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