

If we define precisely what we mean by uncertainties in measurement, we can give a precise statement of the uncertainty principle. If  $\Delta x$  and  $\Delta p$  are defined to be the standard deviations in the measurements of position and momentum, it can be shown that their product must be greater than or equal to  $\hbar/2$ .

$$\Delta x \Delta p_x \geq \frac{1}{2}\hbar \qquad 34-19$$

where  $\hbar = h/2\pi$ .<sup>†</sup>

Equation 34-19 provides a statement of the uncertainty principle first enunciated by Werner Heisenberg in 1927. In practice, the experimental uncertainties are usually much greater than the intrinsic lower limit that results from wave-particle duality.